

**CCE PF  
CCE PR**

ಕರ್ನಾಟಕ ಪ್ರೌಢ ಶಿಕ್ಷಣ ಪರೀಕ್ಷಾ ಮಂಡಳಿ, ಮಲ್ಲೇಶ್ವರಂ, ಬೆಂಗಳೂರು – 560 003

**KARNATAKA SECONDARY EDUCATION EXAMINATION BOARD, MALLESWARAM,  
BANGALORE – 560 003**

ಎಸ್.ಎಸ್.ಎಲ್.ಸಿ. ಪರೀಕ್ಷೆ, ಮಾರ್ಚ್ / ಏಪ್ರಿಲ್ — 2018

**S. S. L. C. EXAMINATION, MARCH/APRIL, 2018**

ಮಾದರಿ ಉತ್ತರಗಳು  
**MODEL ANSWERS**

ದಿನಾಂಕ : 26. 03. 2018 ]

ಸಂಕೇತ ಸಂಖ್ಯೆ : **81-E**

Date : 26. 03. 2018 ]

CODE No. : **81-E**

ವಿಷಯ : ಗಣಿತ

**Subject : MATHEMATICS**

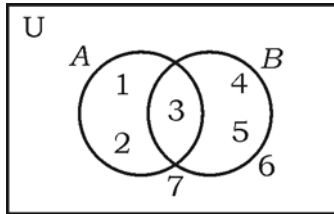
( ಹೊಸ ಪಠ್ಯಕ್ರಮ / New Syllabus )

( ಖಾಸಗಿ ಅಭ್ಯರ್ಥಿ & ಪುನರಾವರ್ತಿತ ಖಾಸಗಿ ಅಭ್ಯರ್ಥಿ / Private Fresh & Private Repeater )

( ಇಂಗ್ಲಿಷ್ ಭಾಷಾಂತರ / English Version )

[ ಗರಿಷ್ಠ ಅಂಕಗಳು : 100

[ Max. Marks : 100

Qn. Nos.	Ans. Key	Value Points	Marks allotted
I. 1.		In the given Venn diagram $n(A)$ is 	
	A	Ans. : 3	1
2.		Sum of all the first 'n' terms of even natural number is Ans. : $n(n+1)$	1

**PF & PR-7008**

[ Turn over

Qn. Nos.	Ans. Key	Value Points	Marks allotted
3.		A boy has 3 shirts and 2 coats. How many different pairs, a shirt and a coat can he dress up with ?  <i>Ans. :</i>	
	C	6	1
4.		In a random experiment, if the occurrence of one event prevents the occurrence of other event is  <i>Ans. :</i>	
	D	mutually exclusive event	1
5.		The polynomial $p(x) = x^2 - x + 1$ is divided by $(x - 2)$ then the remainder is  <i>Ans. :</i>	
	B	3	1
6.		The distance between the co-ordinates of a point $(p, q)$ from the origin is  <i>Ans. :</i>	
	C	$\sqrt{p^2 + q^2}$	1
7.		The equation of a line having slope 3 and $y$ -intercept 5 is  <i>Ans. :</i>	
	D	$y = 3x + 5$	1
8.		The surface area of a sphere of radius 7 cm is	
	B	$616 \text{ cm}^2$ .	1

Qn. Nos.	Value Points	Marks allotted
II.	Answer the following :	$6 \times 1 = 6$
9.	Find the HCF of 14 and 21. Ans. : $14 = 2 \times 7$ $21 = 3 \times 7$ HCF = 7 [ Direct Answer full marks ]	$\frac{1}{2}$ $\frac{1}{2}$ 1
10.	The average runs scored by a batsman in 15 cricket matches is 60 and standard deviation of the runs is 15. Find the coefficient of variation of the runs scored by him. Ans. : $\bar{X} = 60$ $\sigma = 15$ $C.V. = \frac{\sigma}{\bar{X}} \times 100$ $= \frac{15}{60} \times 100$ $= 25.$	$C.V. = \frac{\text{Standard deviation}}{\text{Average}} \times 100$ $= \frac{15}{60} \times 100$ $= 25$ $\frac{1}{2}$ $\frac{1}{2}$ 1
11.	Write the degree of the polynomial $f(x) = x^2 - 3x^3 + 2$ . Ans. : Degree 3	1
12.	What are congruent circles ? Ans. : Circles having same radii } but different centres. } OR Different centres but } same radii }	$\frac{1}{2}$ $\frac{1}{2}$ 1
13.	If $\sin \theta = \frac{5}{13}$ then write the value of cosec $\theta$ . Ans. : $\text{cosec } \theta = \frac{13}{5}$	1

Qn. Nos.	Value Points	Marks allotted
14.	<p>Write the formula used to find the total surface area of a right circular cylinder.</p> <p>Ans. :</p> $TSA = 2\pi r (r + h) \text{ sq.units}$	1
III. 15.	<p>If <math>U = \{0, 1, 2, 3, 4\}</math> and <math>A = \{1, 4\}</math>, <math>B = \{1, 3\}</math> show that <math>(A \cup B)' = A' \cap B'</math>.</p> <p>Ans. :</p> $LHS = (A \cup B)'$ $A \cup B = \{1, 3, 4\}$ $(A \cup B)' = \{0, 2\} \quad \dots (i) \quad \frac{1}{2}$ $RHS = A' \cap B'$ $\left. \begin{array}{l} A' = \{0, 2, 3\} \\ B' = \{0, 2, 4\} \end{array} \right\}$ $A' \cap B' = \{0, 2\} \quad \dots (ii) \quad \frac{1}{2}$ <p>From (i) and (ii)</p> $(A \cup B)' = A' \cap B' \quad \frac{1}{2}$	2
16.	<p>Find the sum of the series <math>3 + 7 + 11 + \dots</math> to 10 terms.</p> <p>Ans. :</p> <p><math>3 + 7 + 11 \dots</math> 10 terms</p> $a = 3$ $d = 4$ $S_n = \frac{n}{2} [2a + (n - 1)d] \quad \frac{1}{2}$	

Qn. Nos.	Value Points	Marks allotted	
	$S_{10} = \frac{10}{2} [2(3) + (10-1)4]$	$\frac{1}{2}$	
	$= \frac{10}{2} [6 + 9(4)]$	}	
	$= \frac{10}{2} [6 + 36]$		$\frac{1}{2}$
	$= 5 \times 42.$		2
	$S_{10} = 210$	$\frac{1}{2}$	
17.	<p>At constant pressure certain quantity of water at <math>24^{\circ}\text{C}</math> is heated. It was observed that the rise of temperature was found to be <math>4^{\circ}\text{C}</math> per minute. Calculate the time required to rise the temperature of water to <math>100^{\circ}\text{C}</math> at sea level by using formula.</p> <p><i>Ans. :</i></p> $a = 24$ $d = 4$ $T_n = 100$ $n = ?$ $T_n = a + (n-1)d$ $100 = 24 + (n-1)4$ $100 = 24 + 4n - 4$ $100 = 20 + 4n$ $n = \frac{80}{4}$ $n = 20. \quad (20-1) = 19 \text{ minutes or } 20\text{th minute}$ <p><i>Alternate Method :</i></p> <p>By taking <math>a = 28</math> and <math>n = 19</math></p> <p style="text-align: center;">OR</p> <p>Any other correct alternate method give marks.</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ 2	

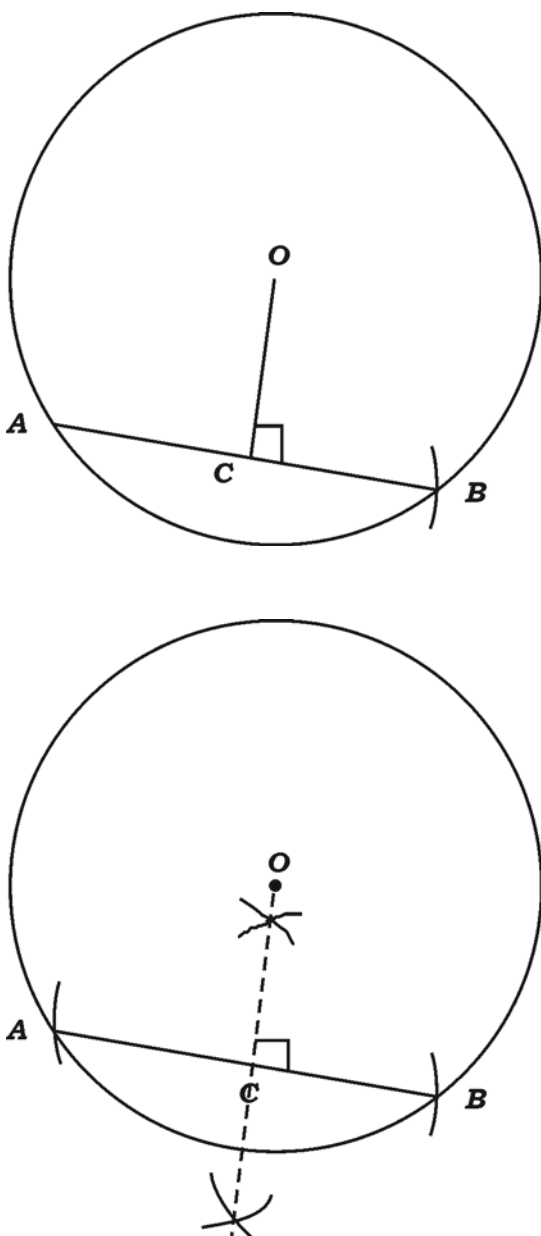
Qn. Nos.	Value Points	Marks allotted
18.	<p>Prove that <math>2 + \sqrt{5}</math> is an irrational number.</p> <p>Ans. :</p> <p>Let us assume <math>2 + \sqrt{5}</math> is rational</p> $2 + \sqrt{5} = \frac{p}{q}, \quad p, q \in \mathbb{Z}, \quad q \neq 0 \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \quad \frac{1}{2}$ $\left. \begin{array}{l} \sqrt{5} = \frac{p}{q} - 2 \\ \sqrt{5} = \frac{p-2q}{q} \end{array} \right\} \quad \frac{1}{2}$ <p><math>\Rightarrow \sqrt{5}</math> is rational</p> <p>but <math>\sqrt{5}</math> is not a rational number <span style="float: right;"><math>\frac{1}{2}</math></span></p> <p>This is against our assumption</p> <p><math>\therefore 2 + \sqrt{5}</math> is an irrational number. <span style="float: right;"><math>\frac{1}{2}</math></span></p>	2
19.	<p>If <math>{}^n P_4 = 20 ({}^n P_2)</math> then find the value of <math>n</math>.</p> <p>Ans. :</p> ${}^n P_4 = 20 {}^n P_2$ $n(n-1)(n-2)(n-3) = 20n(n-1) \quad \left. \begin{array}{l} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \right\} \quad \frac{1}{2}$ $\left. \begin{array}{l} (n-2)(n-3) = 20 \quad \text{OR} \quad (n-2)(n-3) = 5 \times 4 \\ n^2 - 3n - 2n + 6 = 20 \quad \Rightarrow n-2 = 5 \\ n^2 - 5n - 14 = 0 \quad n = 5 + 2 \\ n^2 - 7n + 2n - 14 = 0 \quad \therefore n = 7 \end{array} \right\} \quad 1\frac{1}{2}$ $n(n-7) + 2(n-7) = 0$ $(n-7)(n+2) = 0$ $n-7 = 0 \quad \text{or} \quad n+2 = 0$ $n = 7 \quad \quad \quad n = -2$ <p>( Any alternate method to be considered )</p>	2

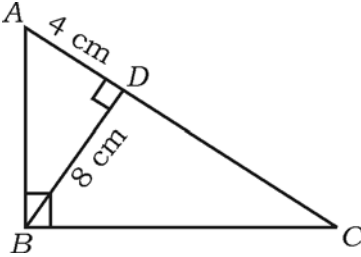
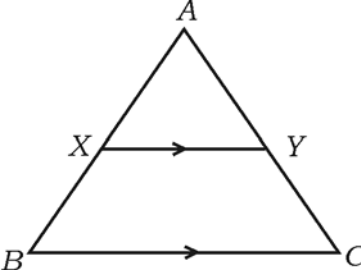
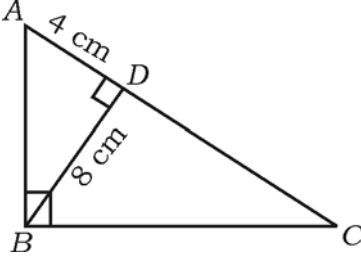
Qn. Nos.	Value Points	Marks allotted												
20.	<p>A die numbered 1 to 6 on its faces is rolled once. Find the probability of getting either an even number or multiple of '3' on its top face.</p> <p>Ans. :</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>S = \{1, 2, 3, 4, 5, 6\}</math></td> <td style="padding: 5px;"><math>\frac{1}{2}</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>n(S) = 6</math></td> <td style="padding: 5px;"><i>This can also be considered</i></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>A = \{2, 3, 4, 6\}</math></td> <td style="padding: 5px;"><math>P(A \cup B) = P(A) + P(B) - P(A \cap B)</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>n(A) = 4</math></td> <td style="padding: 5px;"><math>= \frac{3}{6} + \frac{2}{6} - \frac{1}{6}</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>p(A) = \frac{n(A)}{n(S)}</math></td> <td style="padding: 5px;"><math>= \frac{4}{6}</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>= \frac{4}{6}</math> OR <math>\frac{2}{3}</math></td> <td style="padding: 5px;"><math>\frac{1}{2}</math></td> </tr> </table> <p>( Any other alternate methods give marks )</p>	$S = \{1, 2, 3, 4, 5, 6\}$	$\frac{1}{2}$	$n(S) = 6$	<i>This can also be considered</i>	$A = \{2, 3, 4, 6\}$	$P(A \cup B) = P(A) + P(B) - P(A \cap B)$	$n(A) = 4$	$= \frac{3}{6} + \frac{2}{6} - \frac{1}{6}$	$p(A) = \frac{n(A)}{n(S)}$	$= \frac{4}{6}$	$= \frac{4}{6}$ OR $\frac{2}{3}$	$\frac{1}{2}$	2
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$= \frac{4}{6}$ OR $\frac{2}{3}$	$\frac{1}{2}$													
21.	<p>What are like surds and unlike surds ?</p> <p>Ans. :</p> <p>A group of surds having same order and same radicand in their simplest form. <span style="float: right;"><math>\frac{1}{2} + \frac{1}{2}</math></span></p> <p>Group of surds having different orders or different radicands or both in their simplest form. <span style="float: right;"><math>\frac{1}{2} + \frac{1}{2}</math></span></p>	2												
22.	<p>Rationalise the denominator and simplify :</p> $\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}}$ <p>Ans. :</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} = \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} \times \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} + \sqrt{3}}</math></td> <td style="padding: 5px;"><math>\frac{1}{2}</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>= \frac{(\sqrt{5} + \sqrt{3})^2}{(\sqrt{5})^2 - (\sqrt{3})^2}</math></td> <td style="padding: 5px;"><math>\frac{1}{2}</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>= \frac{5 + 3 + 2\sqrt{15}}{2}</math></td> <td style="padding: 5px;"><math>\frac{1}{2}</math></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>= \frac{8 + 2\sqrt{15}}{2}</math></td> <td style="padding: 5px;"></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;"><math>= 4 + \sqrt{15}</math></td> <td style="padding: 5px;"><math>\frac{1}{2}</math></td> </tr> </table>	$\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} = \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} \times \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} + \sqrt{3}}$	$\frac{1}{2}$	$= \frac{(\sqrt{5} + \sqrt{3})^2}{(\sqrt{5})^2 - (\sqrt{3})^2}$	$\frac{1}{2}$	$= \frac{5 + 3 + 2\sqrt{15}}{2}$	$\frac{1}{2}$	$= \frac{8 + 2\sqrt{15}}{2}$		$= 4 + \sqrt{15}$	$\frac{1}{2}$	2		
$\frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} = \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} \times \frac{\sqrt{5} + \sqrt{3}}{\sqrt{5} + \sqrt{3}}$	$\frac{1}{2}$													
$= \frac{(\sqrt{5} + \sqrt{3})^2}{(\sqrt{5})^2 - (\sqrt{3})^2}$	$\frac{1}{2}$													
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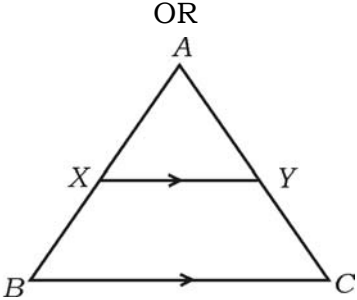
Qn. Nos.	Value Points	Marks allotted																		
23.	<p>Find the quotient and the remainder when</p> <p><math>f(x) = 2x^3 - 3x^2 + 5x - 7</math> is divided by <math>g(x) = (x - 3)</math> using synthetic division.</p> <p style="text-align: center;">OR</p> <p>Find the zeros of the polynomial <math>p(x) = x^2 - 15x + 50</math>.</p> <p>Ans. :</p> <p><math>f(x) = 2x^3 - 3x^2 + 5x - 7</math></p> <p><math>g(x) = x - 3</math></p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding-right: 10px;">3</td> <td style="border: 1px solid black; padding: 5px;">2</td> <td style="border: 1px solid black; padding: 5px;">-3</td> <td style="border: 1px solid black; padding: 5px;">5</td> <td style="border: 1px solid black; padding: 5px;">-7</td> <td></td> </tr> <tr> <td></td> <td colspan="3" style="border: 1px solid black; padding: 5px;">6</td> <td style="border: 1px solid black; padding: 5px;">9</td> <td style="border: 1px solid black; padding: 5px;">42</td> </tr> <tr> <td></td> <td style="border: 1px solid black; padding: 5px;">2</td> <td style="border: 1px solid black; padding: 5px;">3</td> <td style="border: 1px solid black; padding: 5px;">14</td> <td style="border: 1px solid black; padding: 5px;"></td> <td style="border: 1px solid black; padding: 5px;">35</td> </tr> </table> <p><math>q(x) = 2x^2 + 3x + 14</math></p> <p><math>r(x) = 35</math>.</p> <p style="text-align: center;">OR</p> <p><math>f(x) = x^2 - 15x + 50</math></p> <p>At zeroes of the polynomial</p> <p><math>f(x) = 0</math></p> <p><math>x^2 - 15x + 50 = 0</math></p>	3	2	-3	5	-7			6			9	42		2	3	14		35	<p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">2</p>
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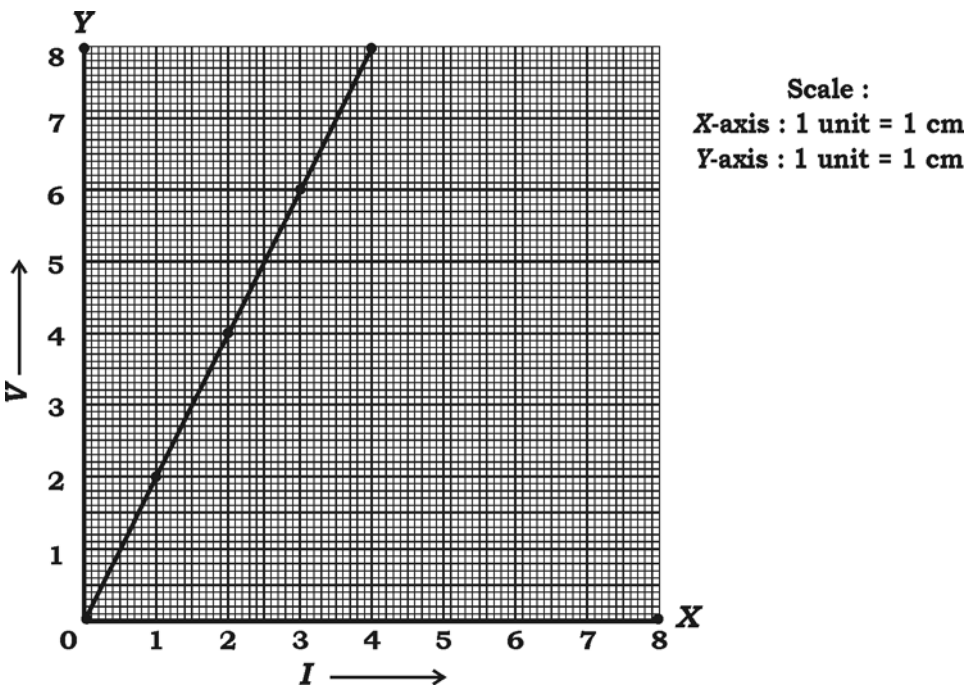


Qn. Nos.	Value Points	Marks allotted
	$x^2 - 10x - 5x + 50 = 0$ $x(x - 10) - 5(x - 10) = 0$ $(x - 10)(x - 5) = 0$ $x - 10 = 0 \quad \text{or} \quad x - 5 = 0$ $x = 10 \quad \quad \quad x = 5$	$\frac{1}{2}$  $\frac{1}{2}$  $\frac{1}{2}$
24.	<p>Solve the equation <math>x^2 - 12x + 27 = 0</math> by using formula.</p> <p>Ans. :</p> <p><math>a = 1, b = -12, c = 27</math></p> $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(1)(27)}}{2(1)}$ $x = \frac{12 \pm \sqrt{144 - 108}}{2}$ $x = \frac{12 \pm \sqrt{36}}{2}$ $x = \frac{12 \pm 6}{2}$ $x = \frac{12 + 6}{2} \quad \text{or} \quad x = \frac{12 - 6}{2}$ $x = \frac{18}{2} \quad \text{or} \quad x = \frac{6}{2}$ $x = 9 \quad \text{or} \quad x = 3$	$\frac{1}{2}$  $\frac{1}{2}$  $\frac{1}{2}$  $\frac{1}{2}$  $\frac{1}{2}$
	<p><math>\therefore</math> The zeroes of the polynomial are 10 and 5.</p>	$\frac{1}{2}$ 2

Qn. Nos.	Value Points	Marks allotted
25.	<p>Draw a chord of length 6 cm in a circle of radius 5 cm. Measure and write the distance of the chord from the centre of the circle.</p> <p>Ans.</p>  <p>Circle <span style="float: right;">1/2</span></p> <p>Chord <span style="float: right;">1/2</span></p> <p>Mid-point marking <span style="float: right;">1/2</span></p> <p>By measuring <math>OC = 4</math> cm. <span style="float: right;">1/2</span></p>	2

Qn. Nos.	Value Points	Marks allotted
26.	<p>In <math>\triangle ABC</math> <math>\angle ABC = 90^\circ</math>, <math>BD \perp AC</math>. If <math>BD = 8</math> cm, <math>AD = 4</math> cm, find <math>CD</math> and <math>AB</math>.</p>  <p style="text-align: center;">OR</p> <p>In <math>\triangle ABC</math>, <math>XY \parallel BC</math> and <math>XY = \frac{1}{2} BC</math>. If the area of <math>\triangle AXY = 10</math> cm<sup>2</sup>, find the area of trapezium <math>XYCB</math>.</p>  <p>Ans. :</p>  $BD^2 = AD \cdot CD \quad \frac{1}{2}$ $8^2 = 4 \cdot CD$ $\frac{64}{4} = CD$ $CD = 16 \text{ cm} \quad \frac{1}{2}$ $\therefore AC = CD + AD = 16 + 4 = 20 \text{ cm}$	

Qn. Nos.	Value Points	Marks allotted
	$AB^2 = AD \cdot AC$ $= 4 \times 20$ $AB^2 = 80$ $AB = \sqrt{80} = \sqrt{16 \times 5} = 4\sqrt{5} \text{ cm}$ <p>( Any other alternate methods give marks )</p> <p style="text-align: center;">OR</p>  <p>Since <math>XY \parallel BC</math></p> $\Delta AXY \sim \Delta ABC$ $\frac{\text{ar}(\Delta AXY)}{\text{ar}(\Delta ABC)} = \frac{XY^2}{BC^2}$ $\frac{\text{ar}(\Delta AXY)}{\text{ar}(\Delta ABC)} = \frac{XY^2}{4XY^2}$ $\frac{10}{\text{ar}(\Delta ABC)} = \frac{1}{4}$ $40 = \text{ar} \Delta ABC$ $\text{ar} \text{ trapezium } XYCB = 40 - 10 = 30 \text{ cm}^2.$	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>2</p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>2</p>
27.	<p>Show that, <math>\cot \theta \cdot \cos \theta + \sin \theta = \text{cosec } \theta</math>.</p> <p>Ans. :</p> $\cot \theta \cdot \cos \theta + \sin \theta = \text{cosec } \theta$ $\text{LHS} = \cot \theta \cdot \cos \theta + \sin \theta$ $= \frac{\cos \theta}{\sin \theta} \cdot \cos \theta + \sin \theta$ $= \frac{\cos^2 \theta + \sin^2 \theta}{\sin \theta}$ $= \frac{1}{\sin \theta}$ $= \text{cosec } \theta.$ <p>( Any other alternate methods give marks )</p>	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>2</p>

Qn. Nos.	Value Points	Marks allotted										
28.	<p data-bbox="284 331 1313 412">A student while conducting an experiment on Ohm's law, plotted the graph according to the given data. Find the slope of the line obtained.</p> <table border="1" data-bbox="446 421 1026 544"><tr><td data-bbox="448 421 678 479"><i>X-axis I</i></td><td data-bbox="678 421 764 479">1</td><td data-bbox="764 421 850 479">2</td><td data-bbox="850 421 936 479">3</td><td data-bbox="936 421 1023 479">4</td></tr><tr><td data-bbox="448 479 678 544"><i>Y-axis V</i></td><td data-bbox="678 479 764 544">2</td><td data-bbox="764 479 850 544">4</td><td data-bbox="850 479 936 544">6</td><td data-bbox="936 479 1023 544">8</td></tr></table>  <p data-bbox="1141 658 1321 750">Scale : X-axis : 1 unit = 1 cm Y-axis : 1 unit = 1 cm</p> <p data-bbox="284 1323 371 1350">Ans. :</p> <p data-bbox="284 1395 572 1429"><math>(x_1, y_1) = (1, 2)</math></p> <p data-bbox="826 1391 1190 1451">Alternate method may be given full marks.</p> <p data-bbox="284 1473 587 1507"><math>(x_2, y_2) = (2, 4)</math></p> <p data-bbox="1278 1473 1313 1507">1/2</p> <p data-bbox="284 1541 539 1626">Slope = <math>\frac{y_2 - y_1}{x_2 - x_1}</math></p> <p data-bbox="1278 1561 1313 1594">1/2</p> <p data-bbox="284 1641 727 1713">Slope = <math>m = \frac{4 - 2}{2 - 1} = \frac{2}{1} = 2</math></p> <p data-bbox="1289 1662 1313 1695">1</p> <p data-bbox="284 1760 1019 1798">Or <math>(x_1, y_1) = (2, 4)</math>      <math>(x_2, y_2) = (3, 6)</math></p> <p data-bbox="284 1845 1019 1883">Or <math>(x_1, y_1) = (3, 6)</math>      <math>(x_2, y_2) = (4, 8)</math></p> <p data-bbox="284 1946 999 1980">Or any two points may be taken to find the slope.</p>	<i>X-axis I</i>	1	2	3	4	<i>Y-axis V</i>	2	4	6	8	2
<i>X-axis I</i>	1	2	3	4								
<i>Y-axis V</i>	2	4	6	8								

Qn. Nos.	Value Points	Marks allotted
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29. Draw the plan for the information given below :

( Scale 20 m = 1 cm )

	Metre To C	
	140	
To D 50	100	40 to B
	60	
To E 30	40	
	From A	

Ans. :

$$40 \text{ m} = \frac{1}{20} \times 40 = 2 \text{ cm}$$

$$60 \text{ m} = \frac{1}{20} \times 60 = 3 \text{ cm}$$

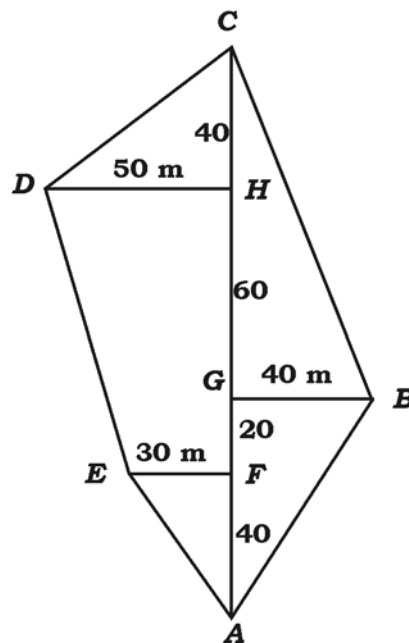
$$100 \text{ m} = \frac{1}{20} \times 100 = 5 \text{ cm}$$

$$140 \text{ m} = \frac{1}{20} \times 140 = 7 \text{ cm}$$

$$30 \text{ m} = \frac{1}{20} \times 30 = 1.5 \text{ cm}$$

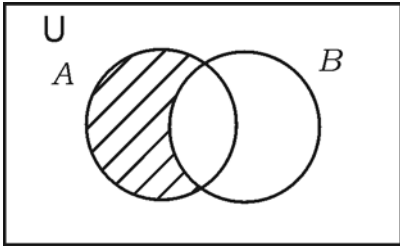
$$50 \text{ m} = \frac{1}{20} \times 50 = 2.5 \text{ cm}$$

1/2




1 1/2

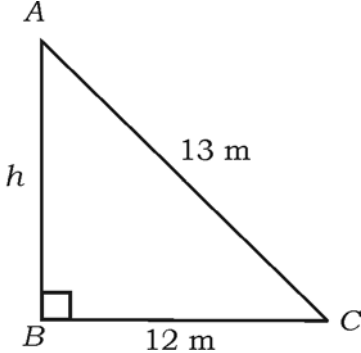
2

Qn. Nos.	Value Points	Marks allotted
30.	<p>Out of 8 different bicycle companies, a student likes to choose bicycle from three companies. Find out in how many ways he can choose the companies to buy bicycle.</p> <p>Ans. :</p> <p>From 8 different bicycle companies he chooses 3 bicycle companies.</p> ${}^8C_3 = \frac{8P_3}{3!}$ $= \frac{8 \times 7 \times 6}{3 \times 2 \times 1}$ $= 56.$ <p style="text-align: right;"><i>Alternate Method :</i></p> ${}^nC_r = \frac{n!}{(n-r)! \cdot r!}$ ${}^8C_3 = \frac{8!}{(8-3)! \cdot 3!}$ $= \frac{8 \times 7 \times 6 \times \cancel{5} \times 4 \times 3 \times 2 \times 1}{5! \times 3 \times 2 \times 1} = 56$	<p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">1/2</p> <p style="text-align: right;">2</p>
31.	<p>If A and B are two non-disjoint sets, draw Venn diagram to represent <math>A \setminus B</math>.</p> <p>Ans. :</p> <div style="text-align: center;">  </div> <p style="text-align: right;">Writing set A &amp; B</p> <p style="text-align: right;">Correct shading</p>	<p style="text-align: right;">1</p> <p style="text-align: right;">1</p> <p style="text-align: right;">2</p>
32.	<p>What is an Arithmetic progression ? Write its general form.</p> <p>Ans. :</p> <p>A sequence in which the consecutive terms either increase or decrease by a fixed number.</p> <p style="text-align: right;">OR</p> <p>An arithmetic progression is a sequence in which each term is obtained by adding a fixed number to the preceding term.</p> $a, a + d, a + 2d, a + 3d \dots$	<p style="text-align: right;">1</p> <p style="text-align: right;">1</p> <p style="text-align: right;">2</p>

Qn. Nos.	Value Points	Marks allotted																									
33.	<p>There are 10 points in a plane such that no three of them are collinear. Find out how many triangles can be formed by joining these points.</p> <p>Ans. :</p> <p><math>n = 10</math></p> <p><math>r = 3</math></p> ${}^n C_r = \frac{n!}{(n-r)!r!} \quad \frac{1}{2}$ ${}^{10} C_3 = \frac{10!}{(10-3)!3!} \quad \frac{1}{2}$ $= \frac{10!}{7!3!} \quad \frac{1}{2}$ $= 120. \quad \frac{1}{2}$ <p>Alternate method :</p> ${}^{10} C_3 = \frac{{}^{10} P_3}{3!}$ $= \frac{10 \times 9 \times 8}{3 \times 2 \times 1}$ $= 120.$	2																									
34.	<p>A student reads the books according to the given data. Draw a pie chart to represent it.</p> <table border="1" data-bbox="288 1308 1289 1451"> <thead> <tr> <th>Name of the books</th> <th>Novels</th> <th>Short stories</th> <th>Magazines</th> <th>Journals</th> </tr> </thead> <tbody> <tr> <td>No. of books</td> <td>10</td> <td>60</td> <td>20</td> <td>30</td> </tr> </tbody> </table> <p>Ans. :</p> <table border="1" data-bbox="300 1496 1219 1886"> <thead> <tr> <th>Name of the books</th> <th>No. of books</th> <th>Central angle</th> </tr> </thead> <tbody> <tr> <td>1. Novels</td> <td>10</td> <td><math>\frac{10}{120} \times 360 = 30^\circ</math></td> </tr> <tr> <td>2. Short stories</td> <td>60</td> <td><math>\frac{60}{120} \times 360 = 180^\circ</math></td> </tr> <tr> <td>3. Magazines</td> <td>20</td> <td><math>\frac{20}{120} \times 360 = 60^\circ</math></td> </tr> <tr> <td>4. Journals</td> <td>30</td> <td><math>\frac{30}{120} \times 360 = 90^\circ</math></td> </tr> </tbody> </table> <p style="text-align: center;">Sum of books = 120</p>	Name of the books	Novels	Short stories	Magazines	Journals	No. of books	10	60	20	30	Name of the books	No. of books	Central angle	1. Novels	10	$\frac{10}{120} \times 360 = 30^\circ$	2. Short stories	60	$\frac{60}{120} \times 360 = 180^\circ$	3. Magazines	20	$\frac{20}{120} \times 360 = 60^\circ$	4. Journals	30	$\frac{30}{120} \times 360 = 90^\circ$	1
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Qn. Nos.	Value Points	Marks allotted
		1
35.	<p>Simplify : <math>\sqrt{75} + \sqrt{108} - \sqrt{192}</math>.</p> <p>Ans. :</p> $\sqrt{75} + \sqrt{108} - \sqrt{192} = \sqrt{25 \times 3} + \sqrt{36 \times 3} - \sqrt{64 \times 3}$ $= 5\sqrt{3} + 6\sqrt{3} - 8\sqrt{3}$ $= 3\sqrt{3}.$	2
36.	<p>A polynomial <math>p(x) = x^2 + 4x + 2</math> is divided by <math>g(x) = (x + 2)</math>. Find the quotient by using division algorithm.</p> <p>Ans. :</p> $P(x) = x^2 + 4x + 2 \qquad g(x) = (x + 2)$ $P(x) = [g(x) * q(x)] + r(x)$ $x^2 + 4x + 2 = [(x + 2)(ax + b)] + r(x)$ $= ax^2 + bx + 2ax + 2b + r(x)$ $x^2 + 4x + 2 = ax^2 + x(b + 2a) + 2b + r(x)$ $\boxed{a = 1} \qquad b + 2a = 4 \qquad 2b + r(x) = 2$ $b = 4 - 2 \qquad \boxed{b = 2} \qquad r(x) = 2 - 4$ $\qquad \qquad \qquad \qquad \qquad \qquad \qquad \boxed{r(x) = -2}$ <p>Quotient = <math>(x + 2)</math></p> <p>Remainder = <math>-2</math></p>	2

Qn. Nos.	Value Points	Marks allotted
37.	<p>If <math>v^2 = u^2 + 2as</math>, solve for <math>v</math> and find the value of <math>v</math>, if <math>u = 0</math>, <math>a = 2</math> and <math>s = 100</math>.</p> <p>Ans. :</p> $v^2 = u^2 + 2as$ $v = \sqrt{u^2 + 2as}$ <p>if <math>u = 0</math>, <math>a = 2</math>, <math>s = 100</math>, <math>v = ?</math></p> $v = \pm \sqrt{0 + 2(2)100}$ $v = \pm \sqrt{400}$ $v = \pm 20.$	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>2</p>
38.	<p>A vertical building casts a shadow of length 12 m. If the distance between the top of the building to the tip of the shadow at a particular time of the day is 13 m. Find the height of the building.</p> <p>Ans. :</p> <div style="text-align: center;">  </div> <p>Height of the building = <math>h</math></p> <p>Length of the shadow = 12 m</p> <p>Distance between top of the building to tip of the shadow = 13 m</p> $AC^2 = AB^2 + BC^2$ $13^2 = h^2 + 12^2$ $169 = h^2 + 144$ $169 - 144 = h^2$ $25 = h^2$ $h = \sqrt{25} = 5 \text{ m}$	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>2</p>

Qn. Nos.	Value Points	Marks allotted
39.	Show that $(\sin \theta + \cos \theta)^2 = 1 + 2 \sin \theta \cos \theta$ . <i>Ans. :</i> L.H.S. = $(\sin \theta + \cos \theta)^2$ = $\sin^2 \theta + \cos^2 \theta + 2 \sin \theta \cdot \cos \theta$ <span style="float:right">1</span> = $1 + 2 \sin \theta \cdot \cos \theta$ <span style="float:right">1</span>	2
40.	Find the co-ordinates of the mid-point of the line segment joining the points ( 14, 12 ) and ( 8, 6 ). <i>Ans. :</i> $x_1 = 14$ $x_2 = 8$ $y_1 = 12$ $y_2 = 6$ $d = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$ <span style="float:right">1/2</span> $d = \left( \frac{14 + 8}{2}, \frac{12 + 6}{2} \right)$ <span style="float:right">1/2</span> = $\left( \frac{22}{2}, \frac{18}{2} \right)$ <span style="float:right">1/2</span> = ( 11 , 9 ) <span style="float:right">1/2</span>	2
IV. 41.	In a Geometric progression the sum of first three terms is 14 and the sum of next three terms of it is 112. Find the Geometric progression. <p style="text-align:center">OR</p> If 'a' is the Arithmetic mean of b and c, 'b' is the Geometric mean of c and a, then prove that 'c' is the Harmonic mean of a and b. <i>Ans. :</i> Let the terms be $a, ar, ar^2, ar^3, ar^4, ar^5$ . $a + ar + ar^2 = 14$ $a(1 + r + r^2) = 14$ <span style="float:right">... (i)          1/2</span> $ar^3 + ar^4 + ar^5 = 112$ $ar^3(1 + r + r^2) = 112$ <span style="float:right">... (ii)          1/2</span>	

Qn. Nos.	Value Points	Marks allotted
	Substitute (i) in (ii) $r^3 (14) = 112$ $r^3 = \frac{112}{14} = 8$ $r = \sqrt[3]{8} = 2$	
	Divide equation (2) by (1) $\frac{ar^3(1+r+r^2)}{a(1+r+r^2)} = \frac{112}{14}$ $r^3 = 8$ $\therefore r = 2$	1
	Substitute $r = 2$ in (i) $a(1+2+2^2) = 14$ $a(7) = 14$ $a = 2$	$\frac{1}{2}$
	$\therefore$ The terms are 2, 4, 8, 16, 32, 64.	$\frac{1}{2}$
	Any other alternate methods can also be considered.	3
	OR	
	$a = \frac{b+c}{2}$	
	$b = \sqrt{ac}$ $b^2 = ac$	$\frac{1}{2}$
	$a = \frac{b+c}{2}$	$\frac{1}{2}$
	$2a = b+c$ $\frac{2ab}{b} = b+c$ [ dividing & multiplying by $b$ in the LHS ]	$\frac{1}{2}$
	OR	
	$2ab = b(b+c)$	
	Multiply RHS & LHS by ' $b$ ' $2ab = b^2 + bc$	$\frac{1}{2}$
	$2ab = ac + bc$	
	$2ab = c(a+b)$	$\frac{1}{2}$
	$\frac{2ab}{a+b} = c$	
	$\therefore c$ is the harmonic mean between $a$ and $b$ .	$\frac{1}{2}$

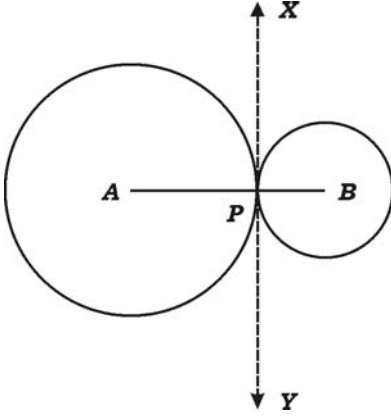
Qn. Nos.	Value Points	Marks allotted																																																
	<p><i>Alternate method :</i></p> $a = \frac{b+c}{2} \quad \dots (i) \qquad b = \sqrt{ac}$ $b^2 = ac$ $b = \frac{ac}{b}$ <p>Substitute <math>b = \frac{ac}{b}</math> in (i)</p> $a = \frac{\frac{ac}{b} + c}{2}$ $2a = \frac{ac + bc}{b}$ $2ab = c(a + b)$ $\frac{2ab}{a+b} = c.$	<p>1</p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>3</p>																																																
42.	<p>Marks scored by 30 students of 10th standard in a unit test of mathematics is given below. Find the variance of the scores :</p> <table border="1" data-bbox="395 1200 1166 1335"> <thead> <tr> <th>Marks (<math>x</math>)</th> <th>4</th> <th>8</th> <th>10</th> <th>12</th> <th>16</th> </tr> </thead> <tbody> <tr> <th>No. of students (<math>f</math>)</th> <td>13</td> <td>6</td> <td>4</td> <td>3</td> <td>4</td> </tr> </tbody> </table> <p><i>Ans. :</i></p> <p><i>Assumed mean method :</i></p> <table border="1" data-bbox="288 1451 1190 1890"> <thead> <tr> <th><math>X</math></th> <th><math>f</math></th> <th><math>d = X - A</math></th> <th><math>fd</math></th> <th><math>d^2</math></th> <th><math>fd^2</math></th> </tr> </thead> <tbody> <tr> <td>4</td> <td>13</td> <td>-6</td> <td>-78</td> <td>36</td> <td>468</td> </tr> <tr> <td>8</td> <td>6</td> <td>-2</td> <td>-12</td> <td>4</td> <td>24</td> </tr> <tr> <td>10</td> <td>4</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>12</td> <td>3</td> <td>2</td> <td>6</td> <td>4</td> <td>12</td> </tr> <tr> <td>16</td> <td>4</td> <td>6</td> <td>24</td> <td>36</td> <td>144</td> </tr> </tbody> </table> <p style="text-align: center;"><math>n = 30 \quad A = 10 \quad \Sigma fd = +60 \quad \Sigma fd^2 = 648</math></p>	Marks ( $x$ )	4	8	10	12	16	No. of students ( $f$ )	13	6	4	3	4	$X$	$f$	$d = X - A$	$fd$	$d^2$	$fd^2$	4	13	-6	-78	36	468	8	6	-2	-12	4	24	10	4	0	0	0	0	12	3	2	6	4	12	16	4	6	24	36	144	<p><math>\frac{1}{2}</math></p>
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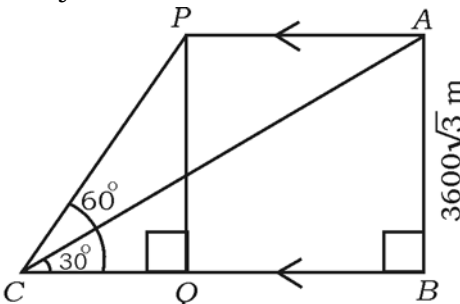
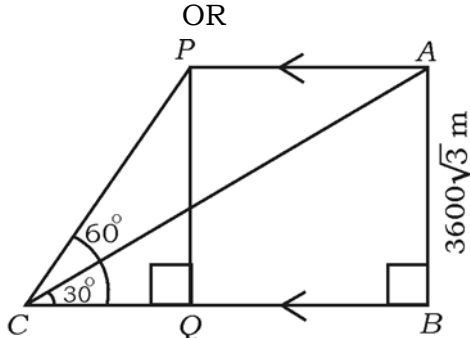
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Qn. Nos.	Value Points	Marks allotted																																				
	$\bar{X} = \frac{\sum fX}{n}$ $= \frac{240}{30} = 8$	1																																				
	$\text{Variance} = \frac{\sum fd^2}{n} = \frac{528}{30}$ $= 17.6$	1/2																																				
	<p><i>Step deviation Method :</i></p> <table border="1" data-bbox="288 775 1193 1155"> <thead> <tr> <th><math>X</math></th> <th><math>f</math></th> <th><math>d = \frac{X-A}{C}</math></th> <th><math>fd</math></th> <th><math>d^2</math></th> <th><math>fd^2</math></th> </tr> </thead> <tbody> <tr> <td>4</td> <td>13</td> <td>-3</td> <td>-39</td> <td>9</td> <td>117</td> </tr> <tr> <td>8</td> <td>6</td> <td>-1</td> <td>-6</td> <td>1</td> <td>6</td> </tr> <tr> <td>10</td> <td>4</td> <td>0</td> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>12</td> <td>3</td> <td>1</td> <td>3</td> <td>1</td> <td>3</td> </tr> <tr> <td>16</td> <td>4</td> <td>3</td> <td>12</td> <td>9</td> <td>36</td> </tr> </tbody> </table>	$X$	$f$	$d = \frac{X-A}{C}$	$fd$	$d^2$	$fd^2$	4	13	-3	-39	9	117	8	6	-1	-6	1	6	10	4	0	0	0	0	12	3	1	3	1	3	16	4	3	12	9	36	3
$X$	$f$	$d = \frac{X-A}{C}$	$fd$	$d^2$	$fd^2$																																	
4	13	-3	-39	9	117																																	
8	6	-1	-6	1	6																																	
10	4	0	0	0	0																																	
12	3	1	3	1	3																																	
16	4	3	12	9	36																																	
	$n = 30 \qquad \qquad \qquad \sum fd^2 = 162$	1																																				
	$A = 10 \qquad \qquad \qquad C = 2$																																					
	$\text{S.D.} = \sqrt{\frac{\sum fd^2}{n} - \left(\frac{\sum fd}{n}\right)^2} \times C$	1/2																																				
	$= \sqrt{\frac{162}{30} - \left(\frac{30}{30}\right)^2} \times 2$																																					
	$= \sqrt{5.4 - 1} \times 2$																																					
	$= \sqrt{4.4} \times 2$																																					
	$= 2.1 \times 2$																																					
	$= 4.2$																																					
	$\therefore \text{Variance } \sigma^2 = (4.2)^2 = 17.6.$	1/2																																				
	<p style="text-align: center;">OR</p> $\text{Variance} = \frac{\sum fd^2}{n} - \left(\frac{\sum fd}{n}\right)^2 \times C^2$ $= \frac{162}{30} - \left(\frac{30}{30}\right)^2 \times 4$ $= (5.4 - 1) \times 4$ $= 4.4 \times 4$ $= 17.6$	1/2																																				

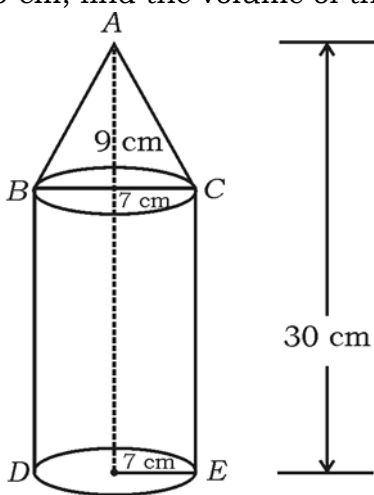
Qn. Nos.	Value Points	Marks allotted
43.	<p>If <math>p</math> and <math>q</math> are the roots of the equation <math>x^2 - 3x + 2 = 0</math>, find the value of <math>\frac{1}{p} - \frac{1}{q}</math>.</p> <p style="text-align: center;">OR</p> <p>A dealer sells an article for Rs. 16 and loses as much per cent as the cost price of the article. Find the cost price of the article.</p> <p>Ans. :</p> $a = 1 \qquad b = -3 \qquad c = 2$ $p + q = \frac{-b}{a} = \frac{-(-3)}{1} = 3 \qquad \frac{1}{2}$ $pq = \frac{c}{a} = \frac{2}{1} = 2 \qquad \frac{1}{2}$ $\frac{1}{p} - \frac{1}{q} = \frac{q - p}{pq} \qquad \frac{1}{2}$ $= \pm \frac{\sqrt{(p+q)^2 - 4pq}}{pq} \qquad \frac{1}{2}$ $= \pm \frac{\sqrt{3^2 - 4(2)}}{2}$ $= \pm \frac{\sqrt{9 - 8}}{2} \qquad \frac{1}{2}$ $= \pm \frac{1}{2} \qquad \frac{1}{2}$ $\frac{1}{p} - \frac{1}{q} = +\frac{1}{2} \text{ or } -\frac{1}{2}$ <p style="text-align: center;">OR</p> <p>C.P. = <math>x</math> S.P. = 16</p> $\text{Loss} = x\% = \frac{x}{100} \times x = \frac{x^2}{100} \quad \left. \vphantom{\text{Loss}} \right\} \begin{array}{l} \text{OR} \\ \frac{x-16}{x} = \frac{x}{100} \\ 100x - 1600 = x^2 \end{array}$ $\text{S.P.} = \text{C.P.} - \text{loss}$ $16 = x - \frac{x^2}{100}$ $1600 = 100x - x^2$	3



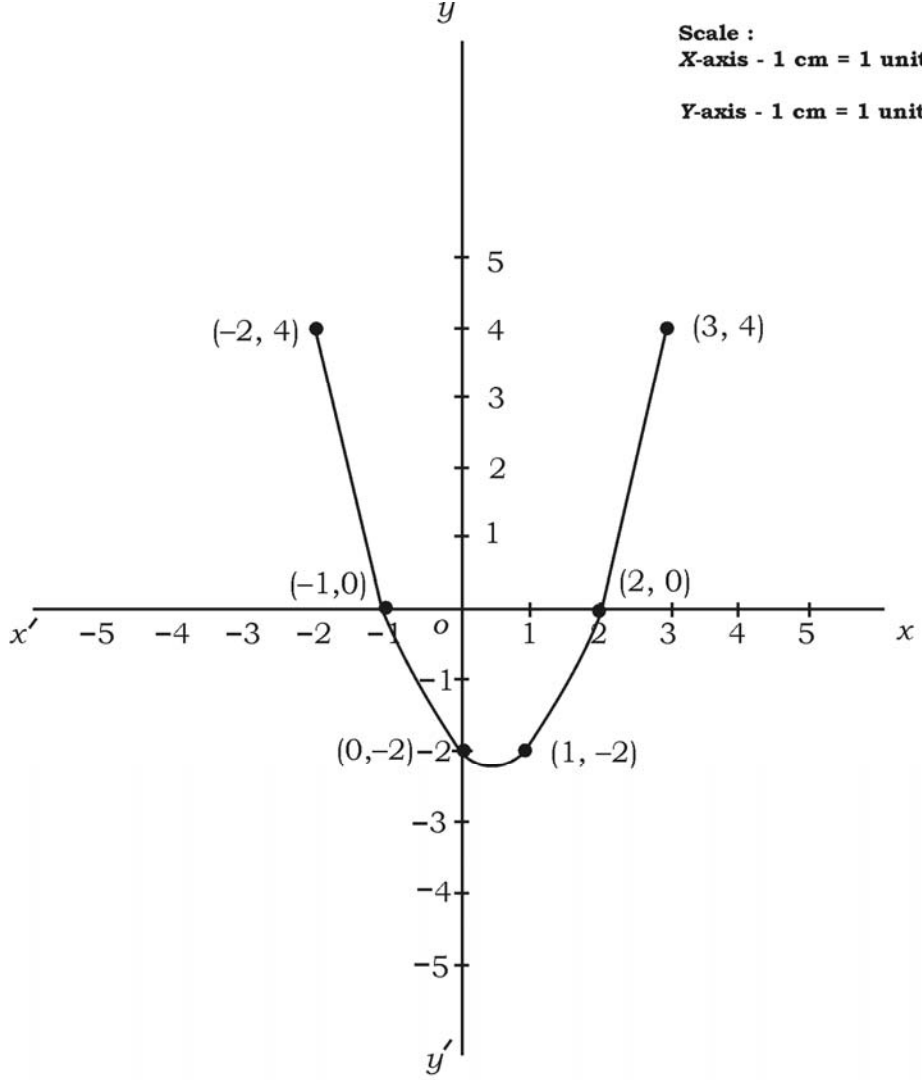
Qn. Nos.	Value Points	Marks allotted
	$x^2 - 100x + 1600 = 0$ $x^2 - 80x - 20x + 1600 = 0$ $x(x - 80) - 20(x - 80) = 0$ $(x - 80)(x - 20) = 0$ $x - 80 = 0$ or $x - 20 = 0$ $x = 80$ $x = 20$	$\frac{1}{2}$          1
	$\therefore$ Cost price is Rs. 80 or Rs. 20.	$\frac{1}{2}$ 3
44.	Prove that, "If two circles touch each other externally, their centres and the point of contact are collinear." <i>Ans. :</i>	
		$\frac{1}{2}$
	<i>Data :</i> <i>A and B are the centres of touching circles, P is the point of contact.</i>	$\frac{1}{2}$
	<i>To prove :</i> <i>A, P and B are collinear.</i>	$\frac{1}{2}$
	<i>Construction :</i> <i>Draw the tangent XY at P.</i>	$\frac{1}{2}$
	<i>Proof :</i> <i>In the figure,</i> $\left. \begin{array}{l} \angle APX = 90^\circ \quad \dots \text{(i)} \\ \angle BPX = 90^\circ \quad \dots \text{(ii)} \end{array} \right\} \begin{array}{l} \text{Radius drawn at the} \\ \text{point of contact is} \\ \text{perpendicular to the} \\ \text{tangent} \end{array}$	$\frac{1}{2}$
	$\angle APX + \angle BPX = 90 + 90$ by adding (i) and (ii)	
	$\angle APB = 180^\circ$ <i>APB is a straight line</i>	$\frac{1}{2}$
	<i>A, P and B are collinear.</i>	3

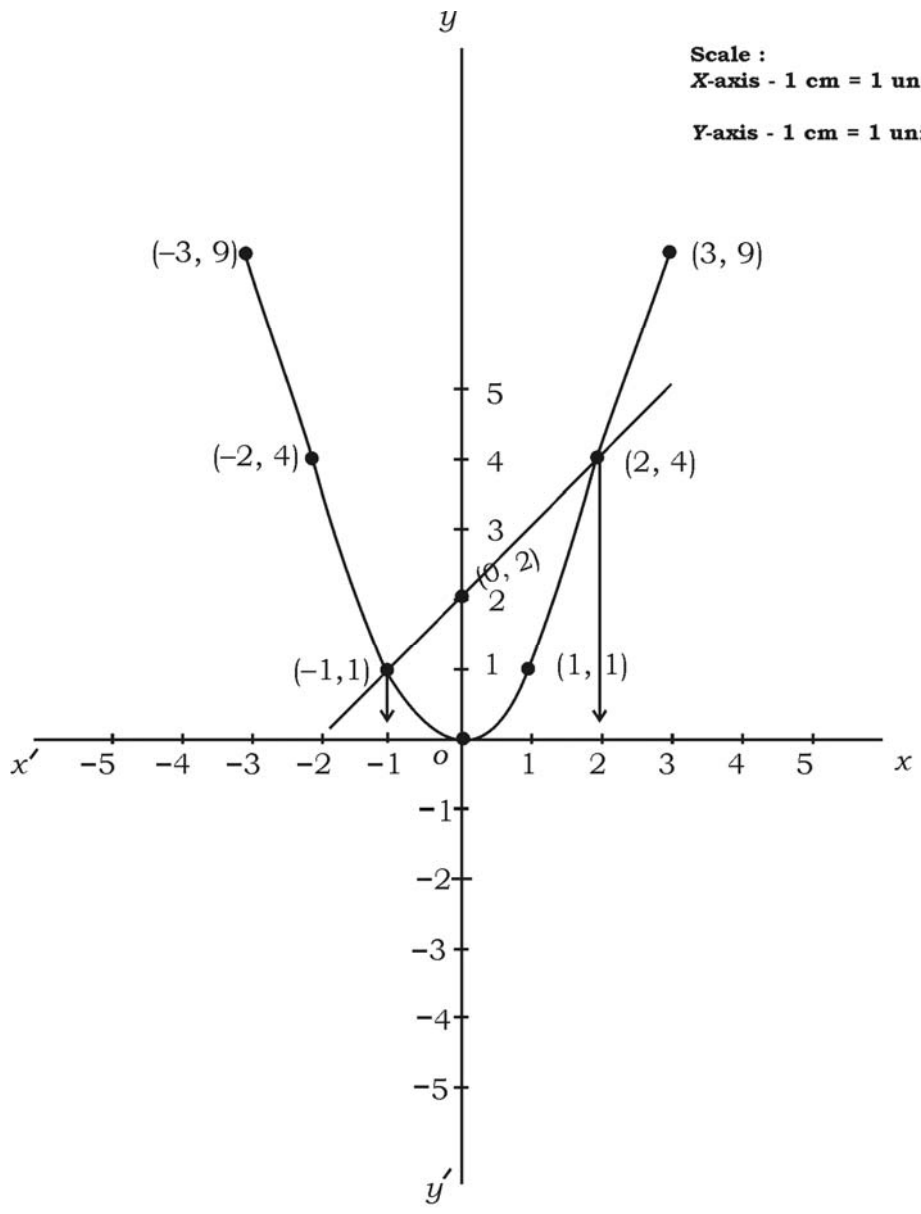
Qn. Nos.	Value Points	Marks allotted
45.	<p>If <math>7 \sin^2 \theta + 3 \cos^2 \theta = 4</math> and '<math>\theta</math>' is acute then show that <math>\cot \theta = \sqrt{3}</math>.</p> <p style="text-align: center;">OR</p> <p>The angle of elevation of an aircraft from a point on horizontal ground is found to be <math>30^\circ</math>. The angle of elevation of same aircraft after 24 seconds which is moving horizontally to the ground is found to be <math>60^\circ</math>. If the height of the aircraft from the ground is <math>3600\sqrt{3}</math> metre. Find the velocity of the aircraft.</p>  <p>Ans. :</p> $4 \sin^2 \theta + 3 \sin^2 \theta + 3 \cos^2 \theta = 4$ $4 \sin^2 \theta + 3 (\sin^2 \theta + \cos^2 \theta) = 4$ $4 \sin^2 \theta + 3 (1) = 4$ $4 \sin^2 \theta = 4 - 3$ $\sin^2 \theta = \frac{1}{4}$ $\sin \theta = \frac{1}{2}$ $\therefore \theta = 30^\circ$ $\therefore \cot \theta = \sqrt{3}.$ <p>Alternate methods can also be considered.</p> <p style="text-align: center;">OR</p>  <p style="text-align: right;">Alternate Method :</p> $7 \sin^2 \theta + 3 \cos^2 \theta = 4 \quad \frac{1}{2}$ $7 \sin^2 \theta + 3 [1 - \sin^2 \theta] = 4$ $7 \sin^2 \theta + 3 - 3 \sin^2 \theta = 4 \quad \frac{1}{2}$ $4 \sin^2 \theta = 1 \quad \frac{1}{2}$ $\sin^2 \theta = \frac{1}{4}$ $\sin \theta = \frac{1}{2} \quad \frac{1}{2}$ $\cos^2 \theta = 1 - \sin^2 \theta \quad \frac{1}{2}$ $\cos \theta = \sqrt{1 - \sin^2 \theta} \quad \frac{1}{2}$ $= \sqrt{1 - \frac{1}{4}}$ $= \frac{\sqrt{3}}{2}$ $\therefore \cot \theta = \frac{\cos \theta}{\sin \theta} = \frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}} = \sqrt{3}$	3

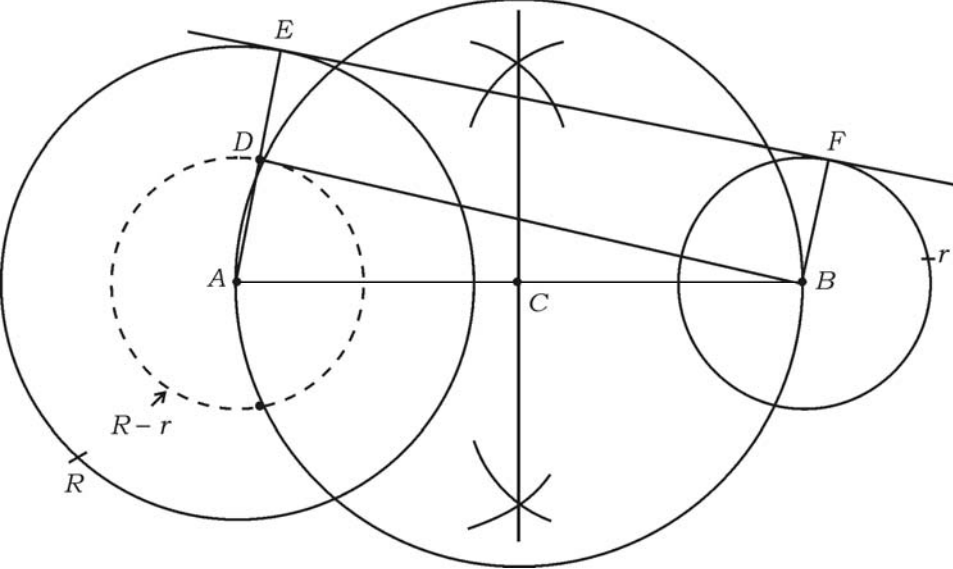
Qn. Nos.	Value Points	Marks allotted
	<p>In <math>\triangle ABC</math>, <math>\angle ABC = 90^\circ</math></p> $\tan \theta = \frac{AB}{BC}$ $\tan 30^\circ = \frac{3600\sqrt{3}}{BC} \quad \frac{1}{2}$ $\frac{1}{\sqrt{3}} = \frac{3600\sqrt{3}}{BC}$ $BC = 3600\sqrt{3} \cdot \sqrt{3} \quad \frac{1}{2}$ $BC = 10800 \text{ m}$ <p>In <math>\triangle PCQ</math>, <math>\angle PQC = 90^\circ</math></p> $\tan \theta = \frac{PQ}{CQ}$ $\tan 60^\circ = \frac{3600\sqrt{3}}{CQ} \quad \frac{1}{2}$ $\sqrt{3} = \frac{3600\sqrt{3}}{CQ}$ $CQ = 3600 \text{ m} \quad \frac{1}{2}$ <p><math>\therefore BQ = BC - CQ = 10800 - 3600</math></p> $BQ = 7200 \text{ m} \quad \frac{1}{2}$ <p><math>\therefore \text{Velocity} = \frac{\text{distance}}{\text{time}} = \frac{d}{t}</math></p> $= \frac{7200}{24}$ $= 300 \text{ m/s} \quad \frac{1}{2}$ <p style="text-align: center;">OR</p> <p>( Any Alternate method )</p>	<p style="text-align: center;">3</p>

Qn. Nos.	Value Points	Marks allotted
46.	<p>A solid is in the form of a cone mounted on a right circular cylinder, both having same radii as shown in the figure. The radius of the base and height of the cone are 7 cm and 9 cm respectively. If the total height of the solid is 30 cm, find the volume of the solid.</p>  <p style="text-align: center;">OR</p> <p>The slant height of the frustum of a cone is 4 cm and the perimeters of its circular bases are 18 cm and 6 cm respectively. Find the curved surface area of the frustum.</p> <p><i>Ans. :</i></p> <p><math>r = 7</math> cm      Let      <math>h_1 = 21</math> cm for cylinder</p> <p><math>r = 7</math> cm           <math>h_2 = 9</math> cm for cone</p> <p>Volume of solid = Volume of cylinder + Volume of cone      <math>\frac{1}{2}</math></p> $= \pi r^2 h_1 + \frac{1}{3} \pi r^2 h_2 \quad \frac{1}{2}$ $= \pi r^2 \left( h_1 + \frac{1}{3} h_2 \right) \quad \frac{1}{2}$ $= \frac{22}{7} \times 7^2 \left( 21 + \frac{1}{3} \times 9 \right) \quad \frac{1}{2}$ $= \frac{22}{7} \times 7 \times 7 (24) \quad \frac{1}{2}$ $= 3696 \text{ c.c.} \quad \frac{1}{2}$ <p>Direct substitution of <math>h_1</math> and <math>h_2</math> value can also be considered.</p> <p style="text-align: center;">OR</p>	3

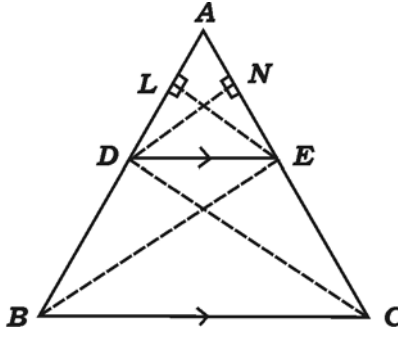
Qn. Nos.	Value Points	Marks allotted														
	$2\pi r_1 = 18 \text{ cm} \qquad 2\pi r_2 = 6 \text{ cm} \qquad l = 4 \text{ cm}$ $r_1 = \frac{18}{2\pi} = \frac{9}{\pi} \text{ cm} \qquad r_2 = \frac{6}{2\pi} = \frac{3}{\pi} \text{ cm}$ <p>Curved Surface Area = <math>\pi (r_1 + r_2) l</math> <span style="float: right;">1</span></p> $= \pi \left( \frac{9}{\pi} + \frac{3}{\pi} \right) 4$ $= 48 \text{ cm}^2.$ <p style="text-align: center;">OR</p> <p>CSA = <math>l [\pi r_1 + \pi r_2]</math></p> $= 4 [9 + 3]$ $= 4 [12]$ $= 48 \text{ cm}^2$	<p style="text-align: right;">1/2</p> <p style="text-align: right;">1 1/2</p> <p style="text-align: right;">3</p>														
<p>V. 47.</p>	<p>Solve the equation <math>x^2 - x - 2 = 0</math> graphically.</p> <p>Ans. :</p> <p>Let <math>y = 0</math></p> $x^2 - x - 2 = 0 \text{ given}$ <p><math>\therefore y = x^2 - x - 2</math></p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td><math>x</math></td> <td>0</td> <td>1</td> <td>-1</td> <td>2</td> <td>3</td> <td>-2</td> </tr> <tr> <td><math>y</math></td> <td>-2</td> <td>-2</td> <td>0</td> <td>0</td> <td>4</td> <td>4</td> </tr> </table> <p>Graph roots</p> <div style="text-align: right; margin-top: 20px;"> <p>Table — 2</p> <p>Parabola — 1</p> <p>Roots — 1/2 + 1/2 4</p> </div>	$x$	0	1	-1	2	3	-2	$y$	-2	-2	0	0	4	4	
$x$	0	1	-1	2	3	-2										
$y$	-2	-2	0	0	4	4										

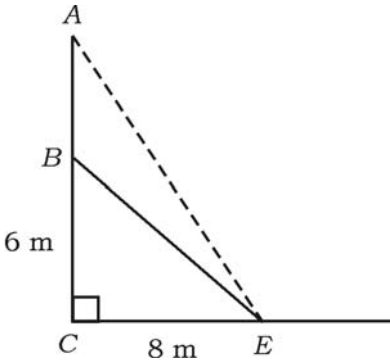
Qn. Nos.	Value Points	Marks allotted																
	<p style="text-align: center;"><math>y</math></p> <p style="text-align: right;">Scale : X-axis - 1 cm = 1 unit Y-axis - 1 cm = 1 unit</p>  <p style="text-align: center;">Roots of the equation are - 1 or 2</p> <p><i>Alternate Method :</i></p> <p>Given <math>x^2 - x - 2 = 0</math></p> $x^2 = x + 2$ <p>Consider <math>y = x^2</math> and <math>y = x + 2</math></p> <p>(i) <math>y = x^2</math></p> <table border="1" data-bbox="300 1836 1066 1948"> <tbody> <tr> <td><math>x</math></td> <td>0</td> <td>1</td> <td>- 1</td> <td>2</td> <td>- 2</td> <td>3</td> <td>- 3</td> </tr> <tr> <td><math>y</math></td> <td>0</td> <td>1</td> <td>1</td> <td>4</td> <td>4</td> <td>9</td> <td>9</td> </tr> </tbody> </table>	$x$	0	1	- 1	2	- 2	3	- 3	$y$	0	1	1	4	4	9	9	
$x$	0	1	- 1	2	- 2	3	- 3											
$y$	0	1	1	4	4	9	9											

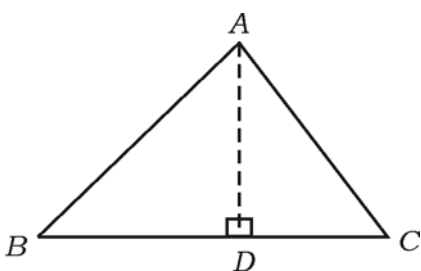
Qn. Nos.	Value Points	Marks allotted												
	<p>(ii) <math>y = x + 2</math></p> <table border="1" data-bbox="300 376 874 492"> <tr> <td><math>x</math></td> <td>0</td> <td>1</td> <td>2</td> <td>-1</td> <td>2</td> </tr> <tr> <td><math>y</math></td> <td>2</td> <td>3</td> <td>4</td> <td>1</td> <td>0</td> </tr> </table> <p style="text-align: right;">                     Tables — 2                      Line — <math>\frac{1}{2}</math>                      Parabola — <math>\frac{1}{2}</math>                      Roots — <math>\frac{1}{2} + \frac{1}{2}</math> </p> <p style="text-align: right;">4</p> <p style="text-align: right;"> <b>Scale :</b>  <b>X-axis - 1 cm = 1 unit</b>  <b>Y-axis - 1 cm = 1 unit</b> </p>  <p style="text-align: center;">Roots of the equation are 2 or -1</p>	$x$	0	1	2	-1	2	$y$	2	3	4	1	0	
$x$	0	1	2	-1	2									
$y$	2	3	4	1	0									

Qn. Nos.	Value Points	Marks allotted								
48.	<p>Construct a direct common tangent to two circles of radii 4 cm and 2 cm whose centres are 9 cm apart. Measure and write the length of the tangent.</p> <p><i>Ans. :</i></p> <p><math>R = 4 \text{ cm}</math>                      <math>r = 2 \text{ cm}</math>                      <math>d = 9 \text{ cm}</math></p> <p><math>R - r = 2 \text{ cm}</math></p>  <p>Length of the tangent = 8.7 cm</p> <table border="0" data-bbox="347 1496 1315 1666"> <tr> <td>Drawing four circles</td> <td style="text-align: right;">2</td> </tr> <tr> <td>Drawing tangents</td> <td style="text-align: right;">1½</td> </tr> <tr> <td>Finding the length</td> <td style="text-align: right;">½</td> </tr> <tr> <td></td> <td style="text-align: right;">4</td> </tr> </table>	Drawing four circles	2	Drawing tangents	1½	Finding the length	½		4	
Drawing four circles	2									
Drawing tangents	1½									
Finding the length	½									
	4									
49.	<p>State and prove Basic Proportionality (Thale's) Theorem.</p> <p><i>Ans. :</i></p> <p>If a straight line is drawn parallel to a side of a triangle, then it divides the other two sides proportionally.</p>	1								



Qn. Nos.	Value Points	Marks allotted
	<div style="text-align: center;">  </div> <p><i>Data :</i> In <math>\triangle ABC</math>, <math>DE \parallel BC</math> }  <i>To prove :</i> <math>\frac{AD}{BD} = \frac{AE}{CE}</math> } <span style="float: right;">1/2</span></p> <p><i>Construction :</i> Join <math>DC</math> and <math>EB</math></p> <p style="padding-left: 100px;">Draw <math>EL \perp AB</math> and <math>DN \perp AC</math>. <span style="float: right;">1/2</span></p> <p><i>Proof :</i></p> $\frac{\text{Area of } \triangle ADE}{\text{Area of } \triangle BDE} = \frac{\frac{1}{2} \times AD \times EL}{\frac{1}{2} \times BD \times EL} \left[ \because A = \frac{1}{2}bh \right] \quad \text{1/2}$ <p><math>\therefore \frac{\triangle ADE}{\triangle BDE} = \frac{AD}{BD} \quad \dots (i)</math></p> $\frac{\text{Area of } \triangle ADE}{\text{Area of } \triangle CDE} = \frac{\frac{1}{2} \times AE \times DN}{\frac{1}{2} \times EC \times DN} \quad \text{1/2}$ $\frac{\triangle ADE}{\triangle CDE} = \frac{AE}{EC}$ <p><math>\Rightarrow \frac{AD}{BD} = \frac{AE}{CE} \quad \left( \because \text{Area } \triangle BDE = \text{area of } \triangle CDE \text{ and Axiom-1} \right) \quad \text{1/2}</math></p>	4

Qn. Nos.	Value Points	Marks allotted
50.	<p>A vertical tree is broken by the wind at a height of 6 metre from its foot and its top touches the ground at a distance of 8 metre from the foot of the tree. Calculate the distance between the top of the tree before breaking and the point at which tip of the tree touches the ground, after it breaks.</p> <p style="text-align: center;">OR</p> <p>In <math>\triangle ABC</math>, <math>AD</math> is drawn perpendicular to <math>BC</math>. If <math>BD : CD = 3 : 1</math>, then prove that <math>BC^2 = 2(AB^2 - AC^2)</math>.</p> <p>Ans. :</p>  <p style="text-align: right;">Fig. : 1</p> <p>In the figure,  Let <math>AC</math> represents the tree <math>h</math>.  <math>B</math> is the point of break <math>BC = 6</math> m  <math>E</math> is the top of the tree touches the ground <math>CE = 8</math> m  <math>AE</math> is the distance between the top of the tree before break and after the break.</p> <p>In <math>\triangle BCE</math>, <math>\angle BCE = 90^\circ</math> <span style="float: right;"><math>\frac{1}{2}</math></span></p> $BE^2 = BC^2 + CE^2$ $BE^2 = 6^2 + 8^2$ <span style="float: right;"><math>\frac{1}{2}</math></span> $BE^2 = 36 + 64$ $BE^2 = 100$ $BE = \sqrt{100} = 10 \text{ m}$ <span style="float: right;"><math>\frac{1}{2}</math></span> $BE = AB = 10 \text{ m}$ <p>( Any other alternate methods give marks )</p>	

Qn. Nos.	Value Points	Marks allotted
	<p>In <math>\triangle ACE</math>, <math>\angle ACE = 90^\circ</math></p> $AE^2 = AC^2 + CE^2$ $= 16^2 + 8^2$ $= 256 + 64$ $AE^2 = 320$ $AE = \sqrt{320}$ $= 8\sqrt{5} \text{ m}$ <p style="text-align: center;">OR</p>  <p style="text-align: right;">Fig. : <math>\frac{1}{2}</math></p> $AB^2 = AD^2 + BD^2 \quad \dots (i)$ $AC^2 = AD^2 + CD^2 \quad \dots (ii)$ <hr style="width: 20%; margin-left: 0;"/> <p>By subtracting</p> $AB^2 - AC^2 = BD^2 - CD^2$ $AB^2 - AC^2 = \left[ \frac{3}{4} BC \right]^2 - \left[ \frac{1}{4} BC \right]^2$ $= \frac{9}{16} BC^2 - \frac{1}{16} BC^2$ $\left( AB^2 - AC^2 \right) = \frac{8 BC^2}{16}$ $= \frac{BC^2}{2}$ $\therefore 2 \left( AB^2 - AC^2 \right) = BC^2$	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>4</p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>4</p>
[ Marks will be given for any alternate method. ]		